

Elementary Analysis For Width/Height Ratio Of Retaining Masonry Structure

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In masonry construction, one of the key challenges is ensuring the stability of structures against lateral forces, such as those caused by wind, water, or soil pressure. Unlike materials like steel or reinforced concrete, masonry is inherently weak in resisting tensile forces. As a result, masonry structures rely primarily on their weight to counteract these lateral loads. To maintain stability and prevent failures such as overturning or sliding, the dimensions of masonry structures must be carefully proportioned.

In this article, we will explore the derivation of an expression for the width-to-height ratio of a simple rectangular masonry structure. This ratio is critical in ensuring that the structure can resist lateral forces purely through its weight. We will examine two scenarios—overturning and sliding—and determine the minimum base width-to-height ratio necessary for the structure's stability, taking into account both the material properties and the frictional resistance at the base.

Calculations

Let,

γ = density of water

s_m = specific gravity of masonry material

s_l = specific gravity of material giving lateral force (e.g. water, soil etc)

h = height of the structure

x = width of the structure

W = weight of structure = $h \cdot x \cdot s_m \cdot \gamma$

μ = coefficient of friction

Case1: For overturning

Moment due to lateral force = moment due to weight of the material

$$\frac{1}{2} \cdot \gamma \cdot s_l \cdot h^2 \cdot \frac{h}{3} = W \cdot \frac{x}{2}$$

$$\frac{1}{2} \cdot \gamma \cdot h^2 \cdot \frac{s_l}{3} = \gamma \cdot s_m \cdot h \cdot x \cdot \frac{x}{2}$$

$$\left(\frac{x}{h}\right)^2 = \left(\frac{s_l}{3 \cdot s_m}\right)$$

$$\frac{x}{h} = \sqrt{\frac{s_l}{3 \cdot s_m}}$$

For water ($s_l=1$); for stone-masonry ($s_m=22/9.81=2.14$):

Therefore,

$$\frac{x}{h} = 0.394 \approx 0.4$$

Case2: For Sliding

Horizontal force = friction factor * weight of the structure

$$\frac{1}{2} \cdot \gamma \cdot s_l \cdot h^2 = \mu \cdot (\gamma \cdot s_m \cdot h \cdot x)$$

$$x/h = sL / (2 * s_m * \mu)$$

For water and stone masonry and using $\mu = 0.65$

$$x/h = 0.359 \approx 0.4$$

Thus from above derivation we see that the minimum base width/height ratio of the rectangular block to resist the lateral (triangular here) force with safety factor 1 is 0.4.

With safety factor of 1.5 the minimum width/height ratio becomes $1.5 * 0.4 = 0.6$.

Other results

